

Theoretical and numerical analysis of the plasma response in a 10-kW class applied-field magnetoplasmadynamic thruster (AF-MPD)

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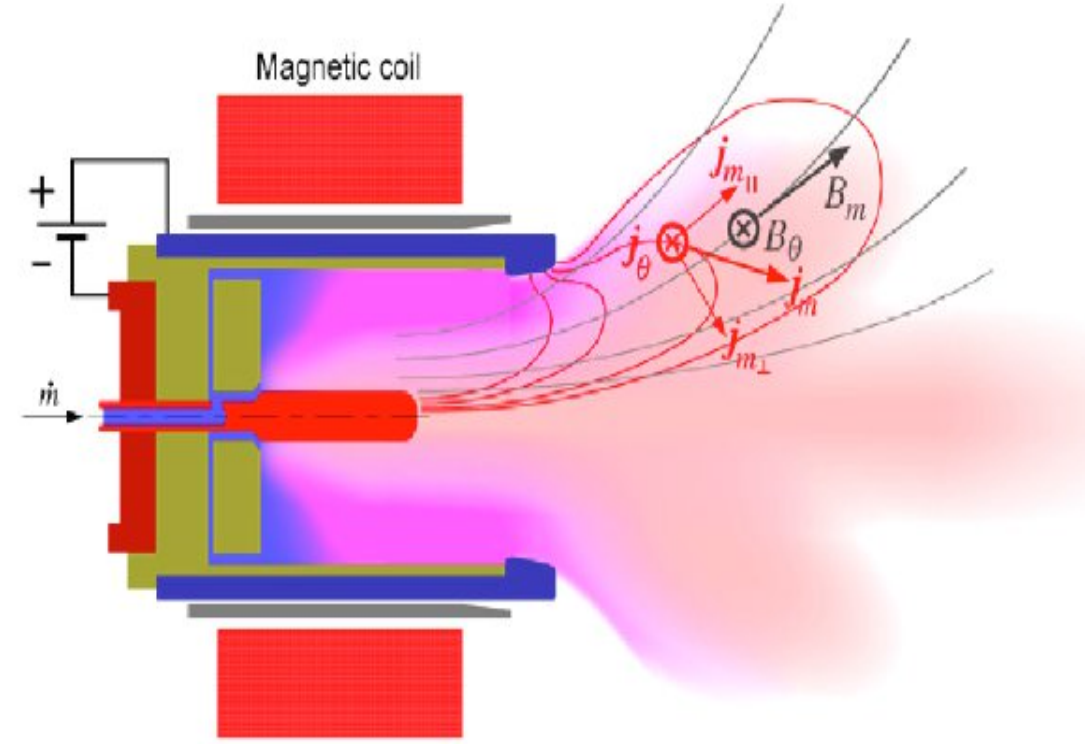
Applied-field Magnetoplasmadynamic thrusters (AF-MPDs)

- Composed of an **annular anode** and a **multichannel tubular cathode**.
- An electrical current is imposed between the two electrodes in order to ionize the propellant which is injected from the backplate and/or from the cathode.
- An **external magnetic field**, supplied by either a coil or a permanent magnet, is used to accelerate the plasma:
 - Both the discharge current j and the applied magnetic field B_a are axial and radial $j = j_z \mathbf{1}_z + j_r \mathbf{1}_r$, $B_a = B_z \mathbf{1}_z + B_r \mathbf{1}_r$.
 - If the magnetic field is strong enough, the plasma undergoes a rotation motion in the θ -direction (Hall current):

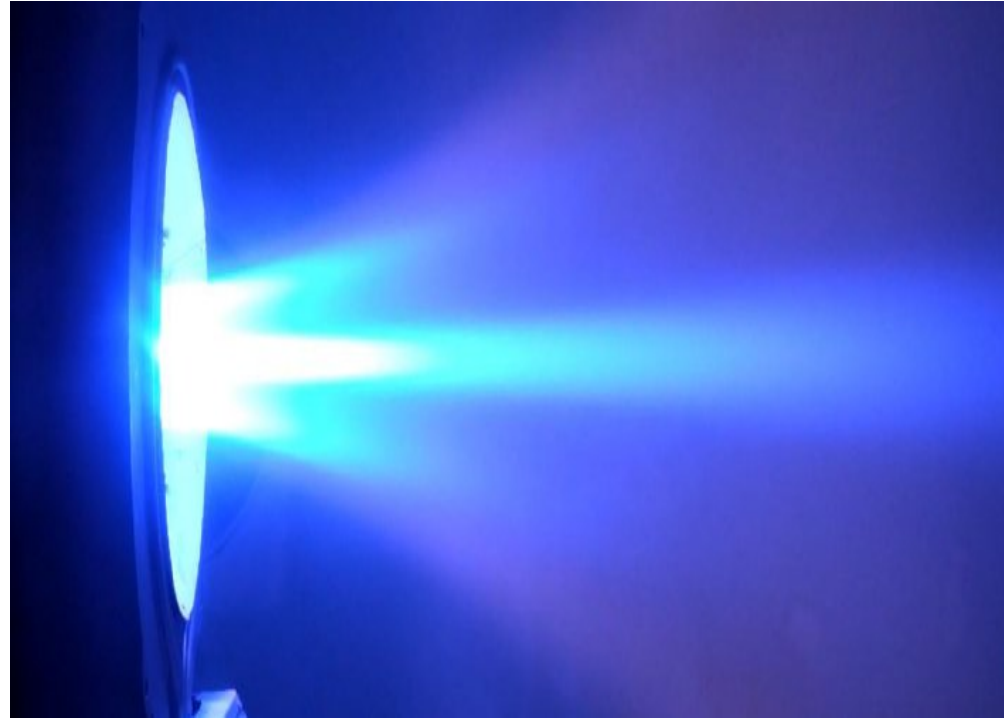
$$j_\theta = \beta_e \frac{j \times B_a}{B_a}$$

where $\beta_e(B_a)$ is called **Hall parameter**.

- The induced Hall current and the applied magnetic field produce both a **pinching** ($F = j_\theta B_z \mathbf{1}_r$) and a **blowing** ($F = j_\theta B_r \mathbf{1}_z$) motion.
- If the discharge current is very high (> 500 A), then the plasma itself generates a magnetic field in the θ -direction strong enough to accelerate the plasma thanks to Lorentz force $F = j \times B_{ind}$.
- In recent years, several **low-power AF-MPD** (< 10 kW) designs employing **hollow cathodes** instead of tubular cathodes have been built and tested.
- As the self-field component is negligible, these thrusters are more similar to Cylindrical Hall Thrusters (CHTs) or Electrodeless Plasma Thrusters (EPTs).
- Experimental evidences shows that **performances of low-power AF-MPDs are poor**.



Andrenucci (2010). Encyclopedia of Aerospace Engineering



Boxberger et al. (2017). Integral Measurements of 100 kW Class Steady State Applied-Field Magnetoplasmadynamic Thruster SX3 and Perspectives of AF-MPD Technology

Research gap and Objectives

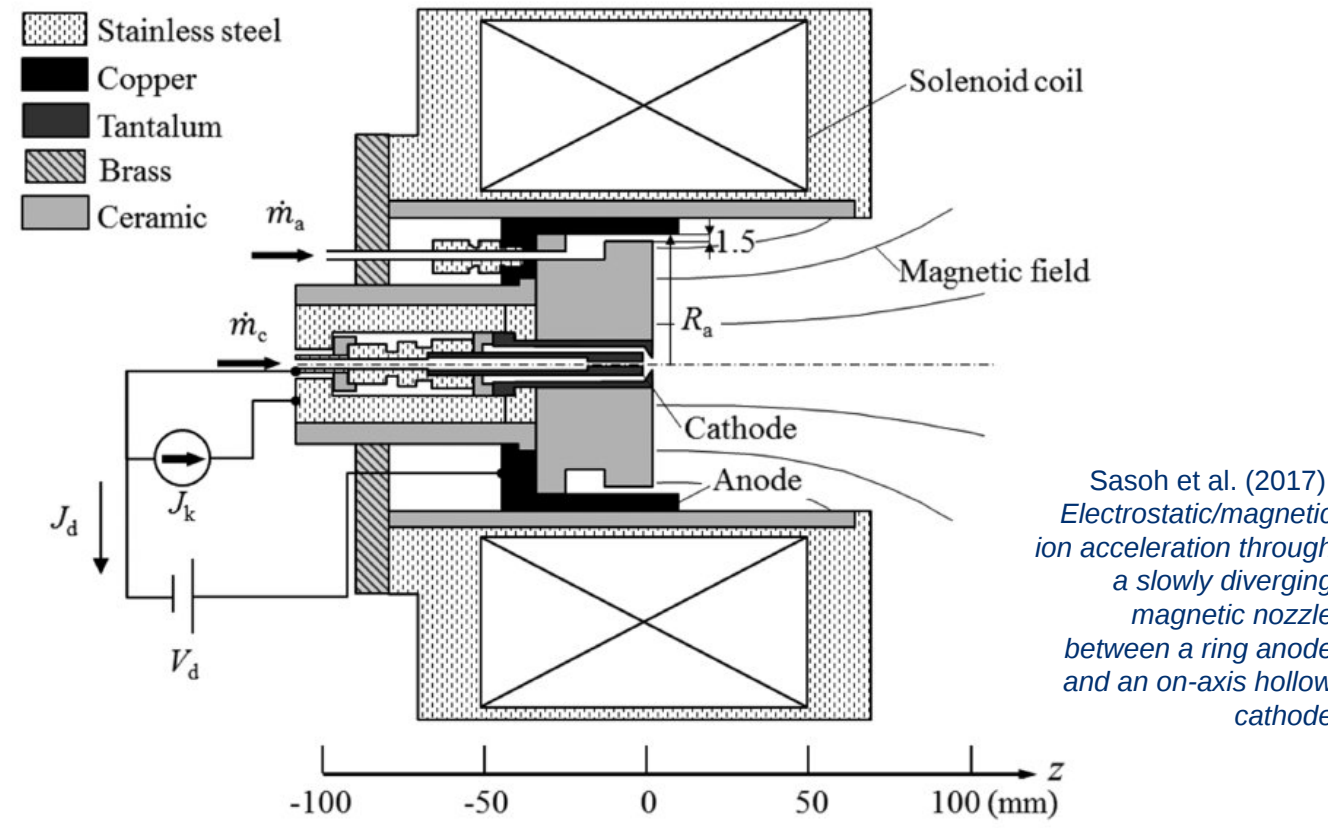
- Several authors have proposed **models to estimate the thrust** of AF-MPDs. However, the underlying physical mechanisms responsible for plasma acceleration are still not fully understood.
- Scaling laws** for AF-MPD thrusters are **inaccurate** in predicting the performances in terms of the geometry and of the operative parameters, especially for in the low-power regime.
- Technical literature on numerical simulations** of AF-MPD thrusters is practically inexistent.

The thesis aims at:

- Characterizing the acceleration mechanisms** of low-power AF-MPD thrusters, which are still unclear.
- Analyzing the plasma response to **identify sources of efficiency losses** to improve future designs.
- Comparing the performances** with other classes of plasma thrusters such as Hall thrusters, Cylindrical Hall thrusters and Electrodeless Plasma Thrusters, and high power AF-MPDs.

Methodology and preliminary results

- Numerical simulations have been performed with **HYPHEN**, an in-house made 2D axisymmetric hybrid code.
- HYPHEN adopts a **Particle in Cell (PIC)** model for heavy species (ions, neutrals) for which a **cartesian mesh** is used and a fluid model for electrons which employs a so-called **Magnetic Field Aligned Mesh (MFAM)** to reduce numerical diffusion.
- A **xenon-fed low-power AF-MPD** design proposed by Sasoh et al. has been simulated.

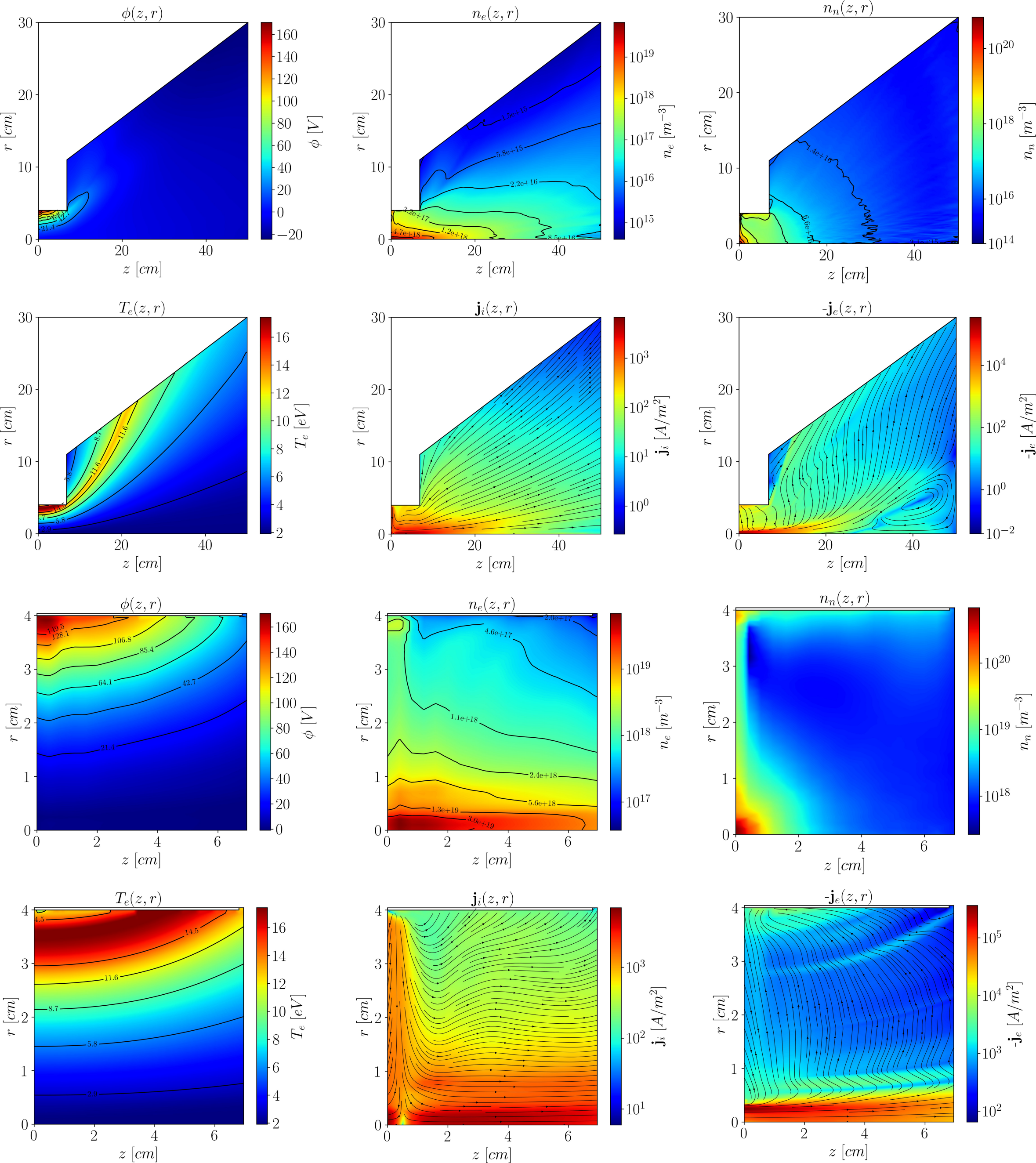


Sasoh et al. (2017). Electrostatic/magnetic ion acceleration through a slowly diverging magnetic nozzle between a ring anode and an on-axis hollow cathode

$\dot{m}_a$	$\dot{m}_c$	V_d	B_a	J_d	F	I_{sp}	P_d	η_t
2.73 mg/s	0.49 mg/s	150 V	0.2 T	6.2 A	26.9 mN	835 s	930 W	0.121

Simulation results

Plasma response



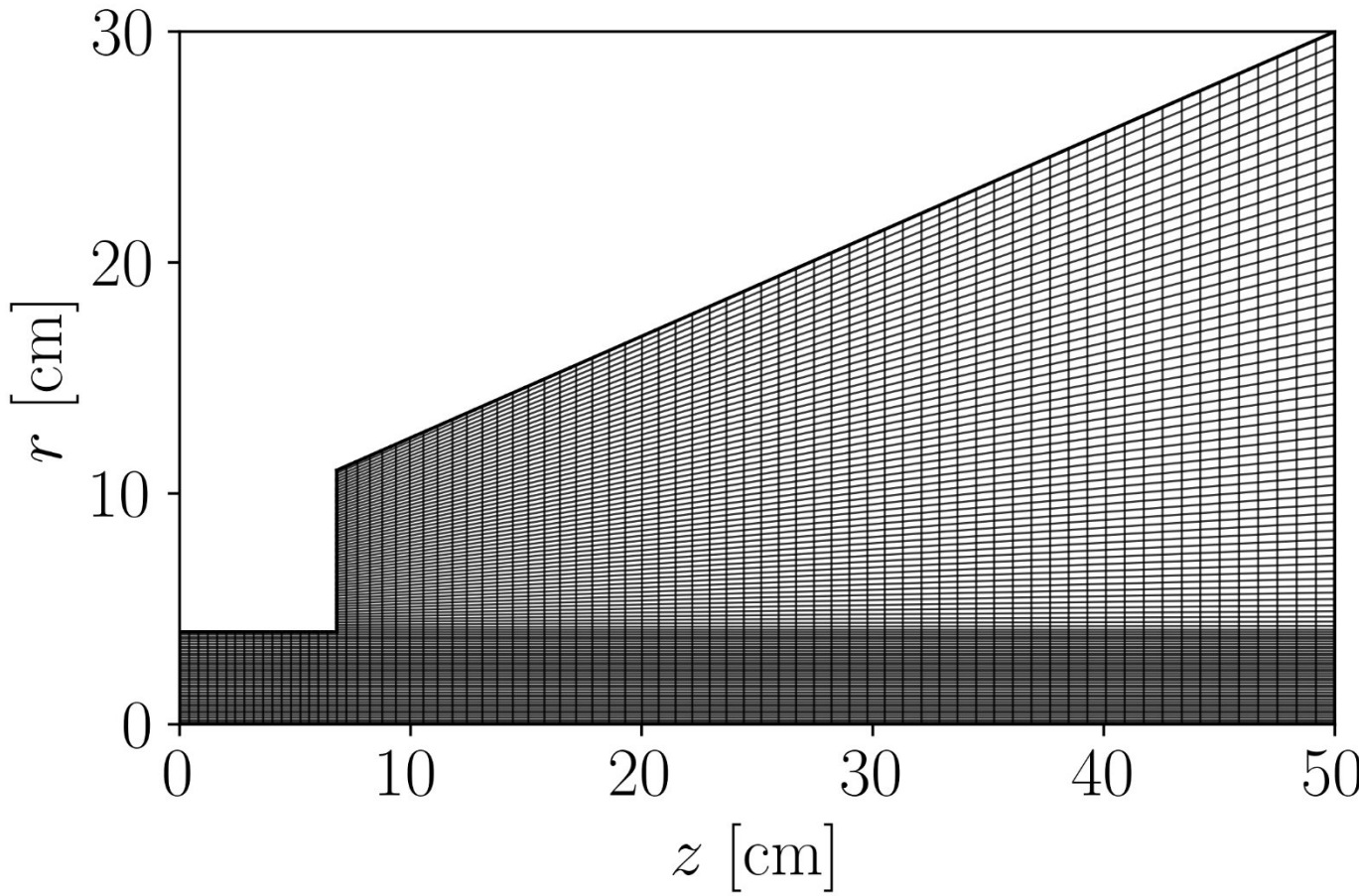
Propulsive performances

F	I_d	P_d
27.32 mN	6.44 A	994.12 W

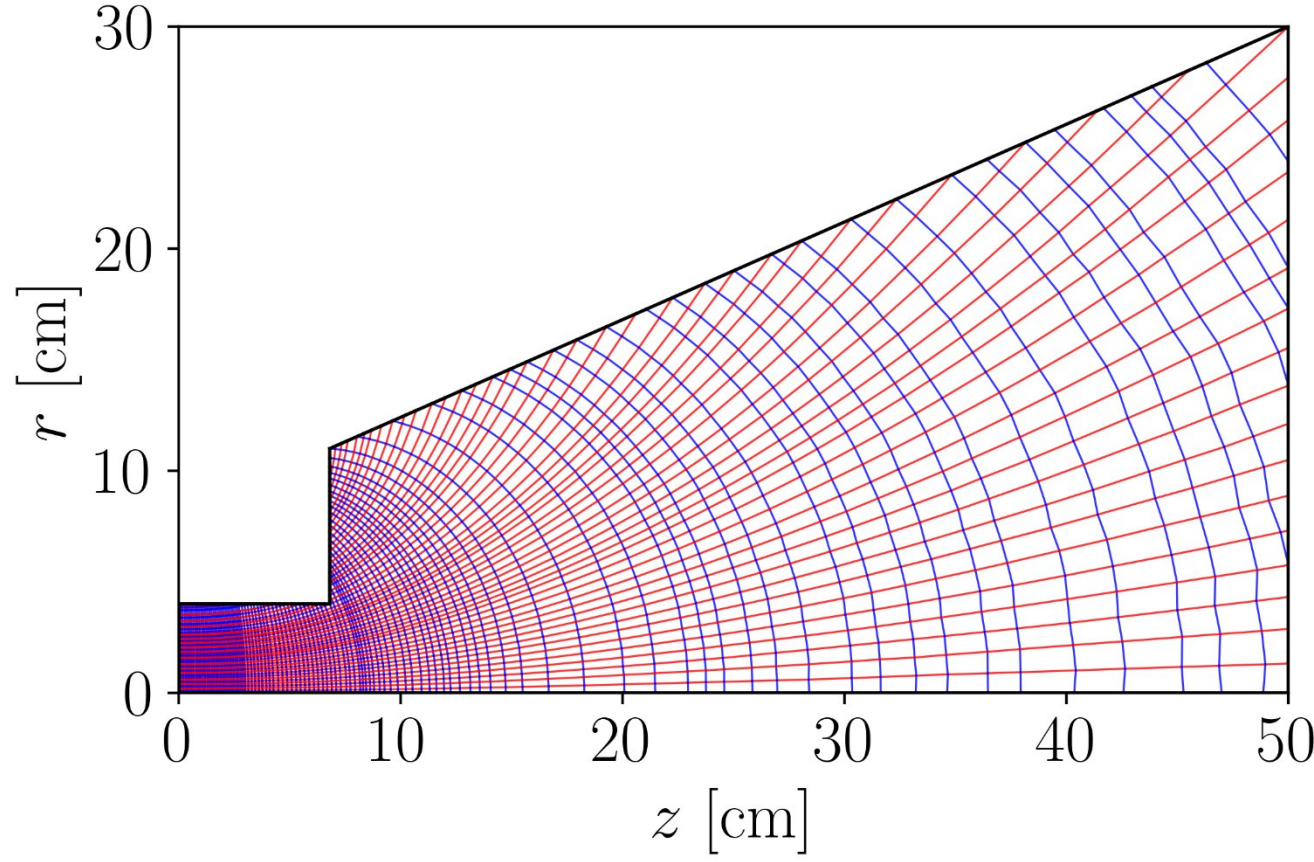
η_t	η_{ene}	η_{div}	η_{disp}	η_u	η_{cur}	η_{prod}
0.117	0.307	0.508	0.746	0.961	0.398	0.343

Simulation setup

PIC mesh



MFAM



Simulation parameters

Domain size (z, r)	(50, 30) cm
PIC mesh number of cells	6521
MFAM number of cells	2929
Ion-moving time step	15 ns
Simulation steps	90000
Injected Xe velocity	300 m/s
Injection Xe temperature	850 K
Walls accommodation factor	1

Reaction set

$\text{Xe} + e^- \rightarrow \text{Xe}^+ + 2e^-$	$\text{Xe}^{2+} + e^- \rightarrow \text{Xe}^{3+} + 2e^-$
$\text{Xe} + e^- \rightarrow \text{Xe}^{2+} + 3e^-$	$\text{Xe}(s) + \text{Xe}^+(f) \rightarrow \text{Xe}^+(s) + \text{Xe}(f)$
$\text{Xe} + e^- \rightarrow \text{Xe}^{3+} + 4e^-$	$\text{Xe}(f) + e^- \rightarrow \text{Xe}^+ + 2e^-$
$\text{Xe}^+ + e^- \rightarrow \text{Xe}^{2+} + 2e^-$	$\text{Xe}^+(s) + e^- \rightarrow \text{Xe}^{2+} + 2e^-$
$\text{Xe}^+ + e^- \rightarrow \text{Xe}^{3+} + 3e^-$	$\text{Xe}^+(s) + e^- \rightarrow \text{Xe}^{3+} + 3e^-$